

# Measuring tissue stiffness using ultrasound

## Final Project Presentation

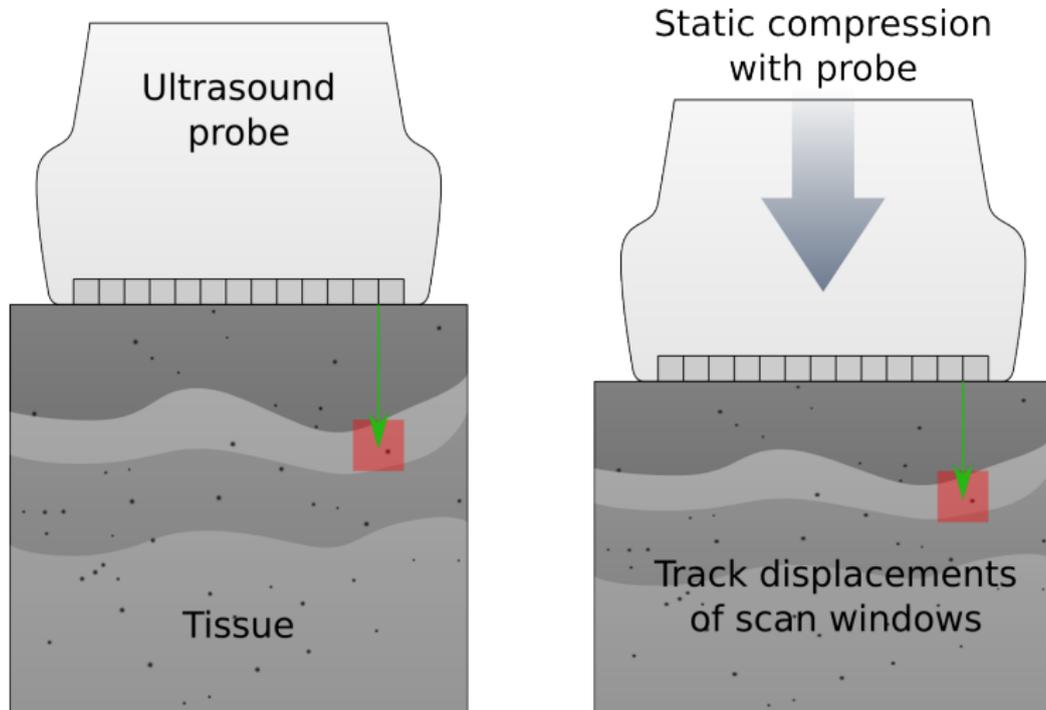
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# Motivation

- Elastic properties of tissue characteristic of some structures and pathologies
- Manual palpation - effective, but only for large near-surface structures
- Ultrasound elastography - images of tissue stiffness

# Quasi-static ultrasound elastography





# Quasi-static ultrasound elastography

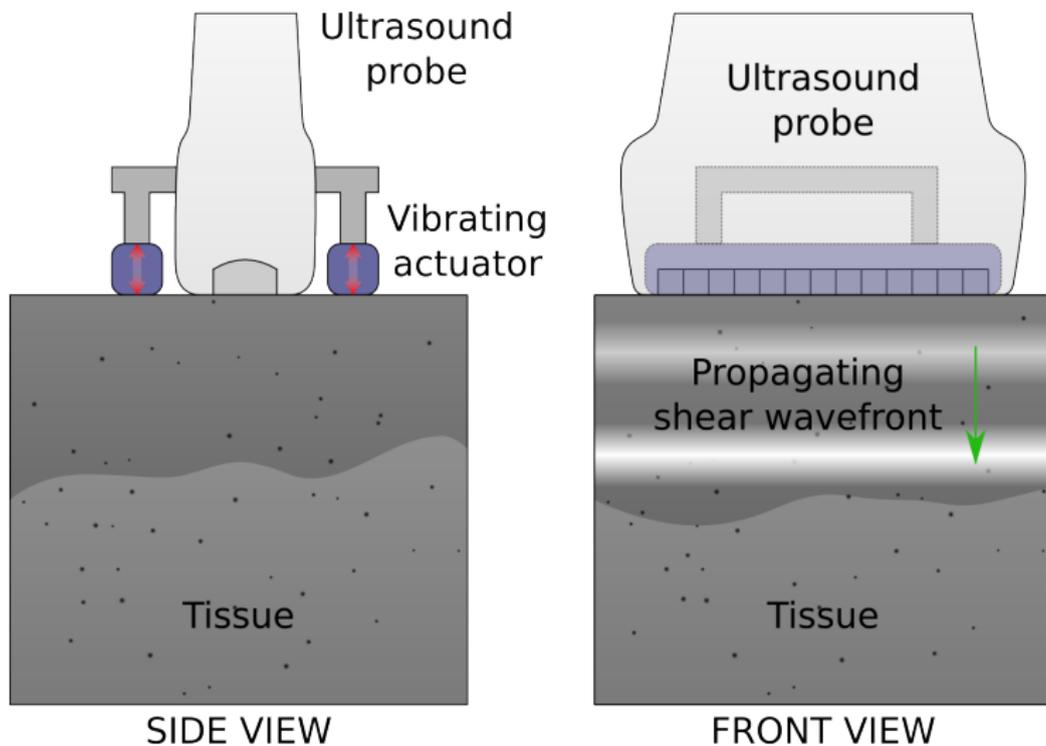
## Advantage

- Requires only standard ultrasound hardware (software-based)

## Disadvantage

- Gives only relative stiffness values - qualitative assessment only

# Dynamic ultrasound elastography





# Dynamic ultrasound elastography

## Advantage

- Absolute stiffness values - quantitative assessment possible

## Disadvantage

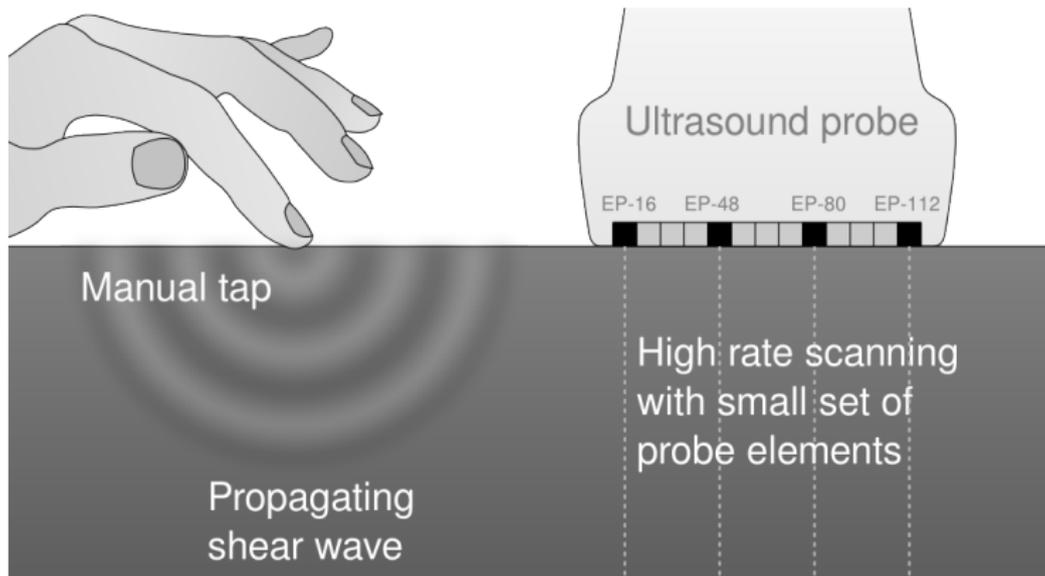
- Requires specialist hardware

# Project aim

To develop an ultrasound elastography method which:

gives **absolute estimates of tissue stiffness**  
using only **standard ultrasound hardware**

# Proposed method



# Estimating stiffness: arrival time method

## Shear wave speed

$$c_s = \sqrt{\frac{E}{3\rho}}$$

( $c_s$  - shear wave speed,  $\rho$  - density,  $E$  - elastic modulus)

Cross-correlation based tracking of wave fronts  $\Rightarrow$

Differences in arrival time of wave at different scan points  $\Rightarrow$

Wave velocities from known separations of scan elements  $\Rightarrow$

Elastic moduli ( $\sim$  stiffness)

# Estimating stiffness: inversion method

## Governing equation of motion

$$\rho \frac{\partial^2 u}{\partial t^2} = \frac{E}{3} \nabla^2 u$$

( $u$  - displacements,  $t$  - time,  $\rho$  - density,  $E$  - elastic modulus)

## Algebraic inversion under model assumptions

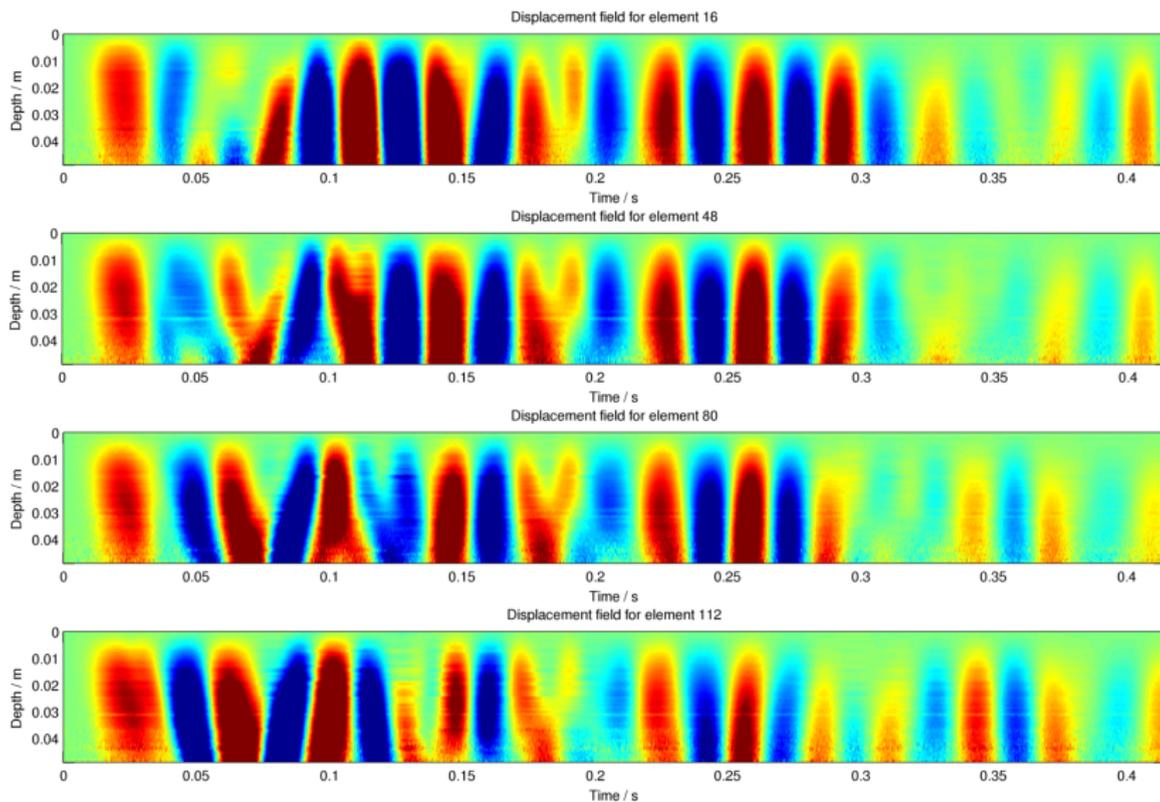
$$E \approx \frac{3}{n} \sum_{i=0}^n \rho \frac{\frac{\partial^2 u_i}{dt^2}}{\frac{\partial^2 u_i}{\partial x^2} + \frac{\partial^2 u_i}{\partial z^2}}$$

# Tests with tissue mimicking phantom



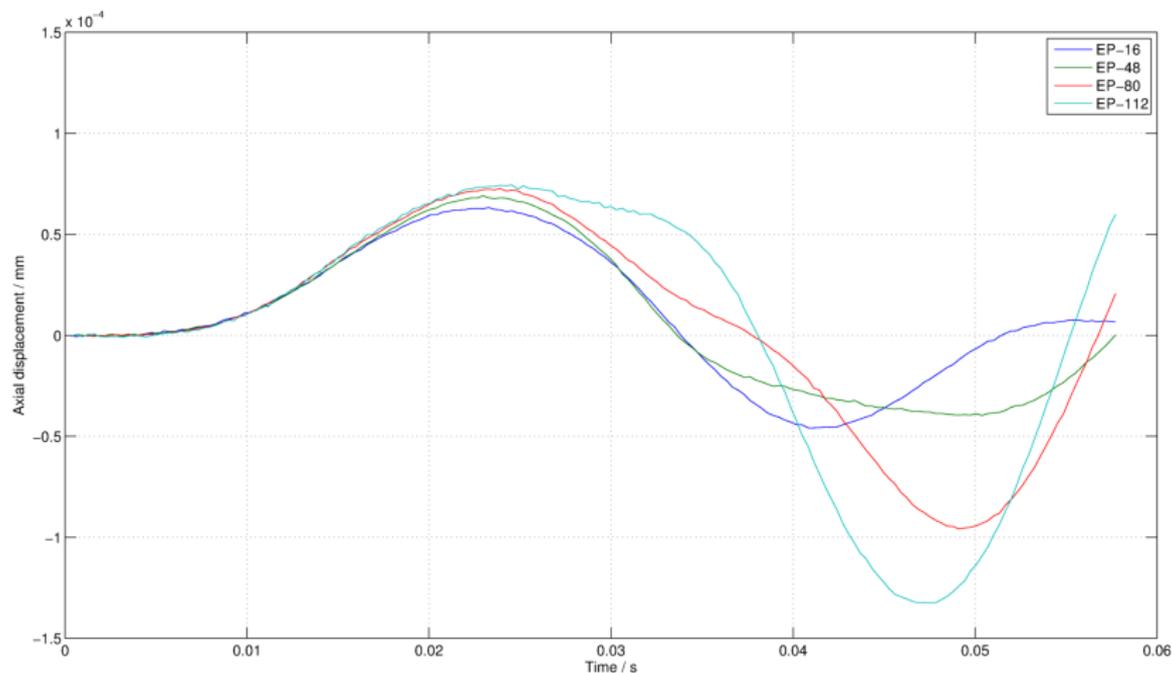


# Tests with tissue mimicking phantom





# Tests with tissue mimicking phantom

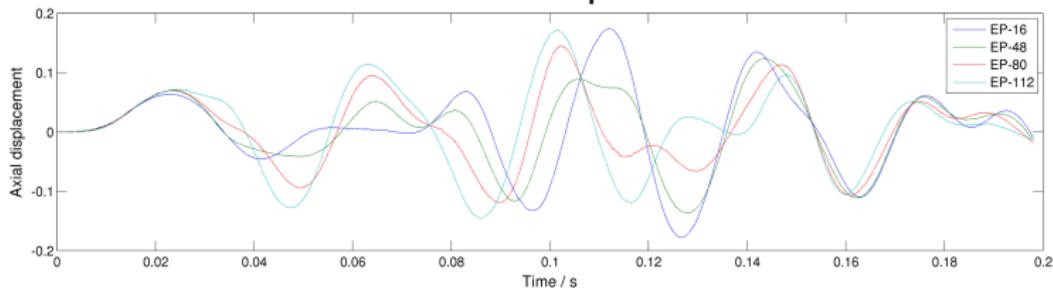




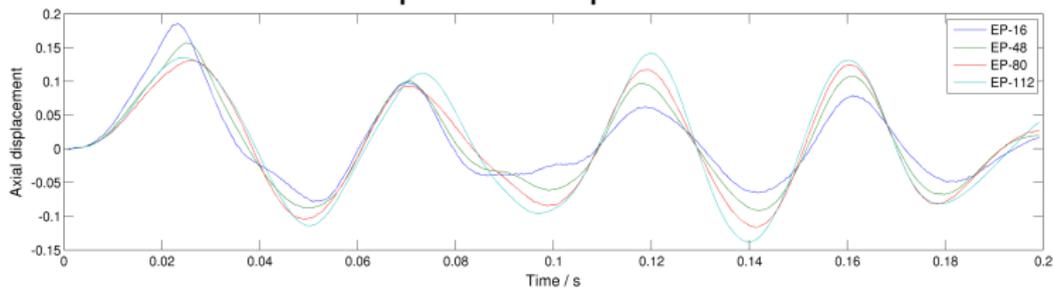


# Probe motion

## Probe in contact with phantom surface

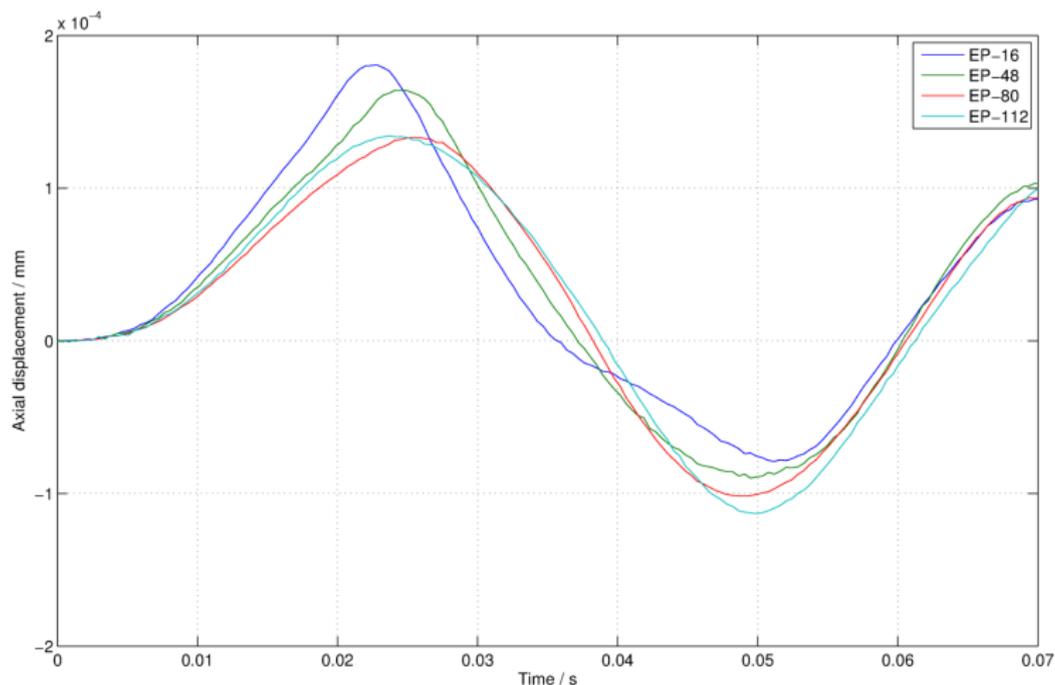


## Probe decoupled from phantom surface





# Probe motion



Displacement responses with probe decoupled from phantom surface

# Wave propagation theory

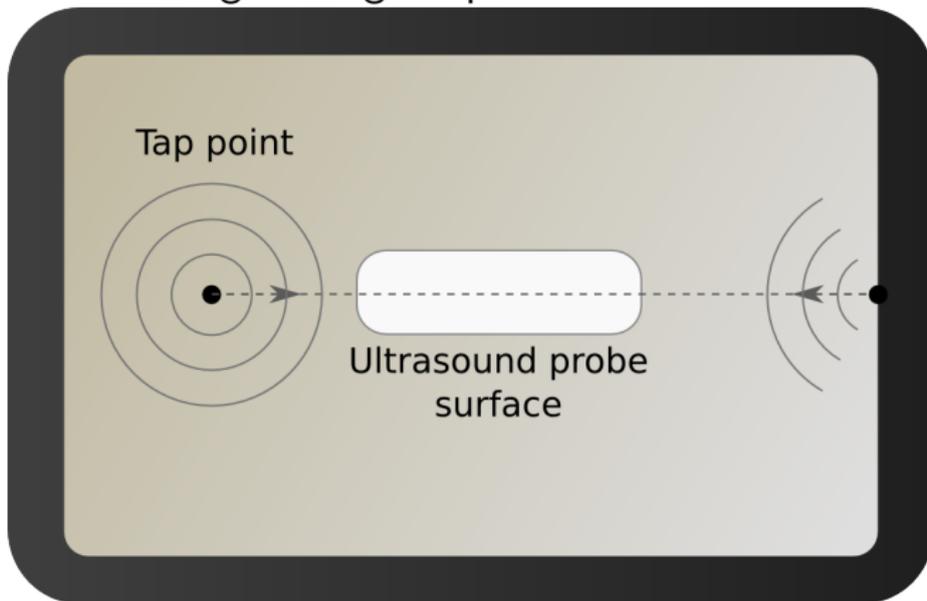
- Vector displacement field  $\mathbf{u}$  combination of irrotational component  $\nabla\phi$  and equivoluminal component  $\nabla \times \mathbf{p}$

$$\mathbf{u} = \nabla\phi + \nabla \times \mathbf{p}$$

- Typical distinction between shear and compressional waves misleading
- Wave velocity dependent on wavefront and medium geometry,  $\sqrt{\frac{E}{3\rho}}$  only a lower bound
- Minimising reflections and resulting interference reduces discrepancy

# Wave reflections

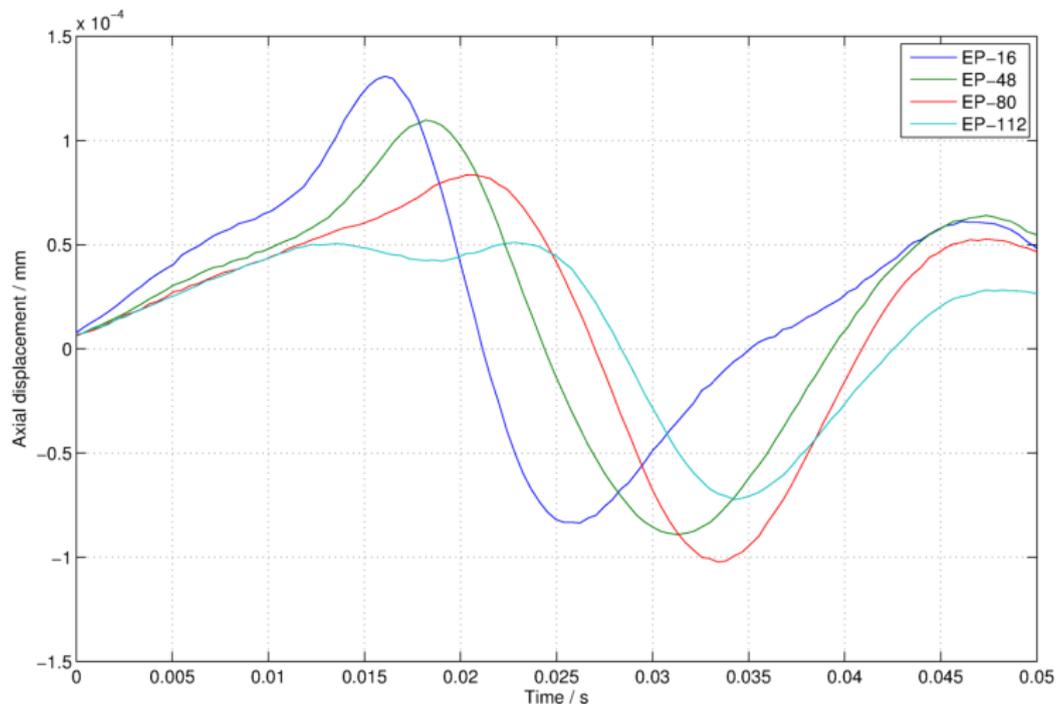
Original aligned probe orientation







# Wave reflections



Displacement responses with probe angled to phantom walls

## Results and conclusions

	Phantom		Calf muscle	
	$c_s / \text{ms}^{-1}$	$E / \text{kPa}$	$c_s / \text{ms}^{-1}$	$E / \text{kPa}$
Actual	2.9	25	2.3*	15*
Estimated	3.9	45	3.6	38

(\* *typical figure*)

- Plausible shear modulus values measured in phantom and in-vivo
- Attempts at localisation not successful
- Unclear whether direct inversion viable

# Thank-you

## Any questions?